



# ULTIMATE Automating SMT



[ultimate.informatik.uni-freiburg.de](http://ultimate.informatik.uni-freiburg.de)

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[github.com/ultimate-pa/ultimate](https://github.com/ultimate-pa/ultimate)

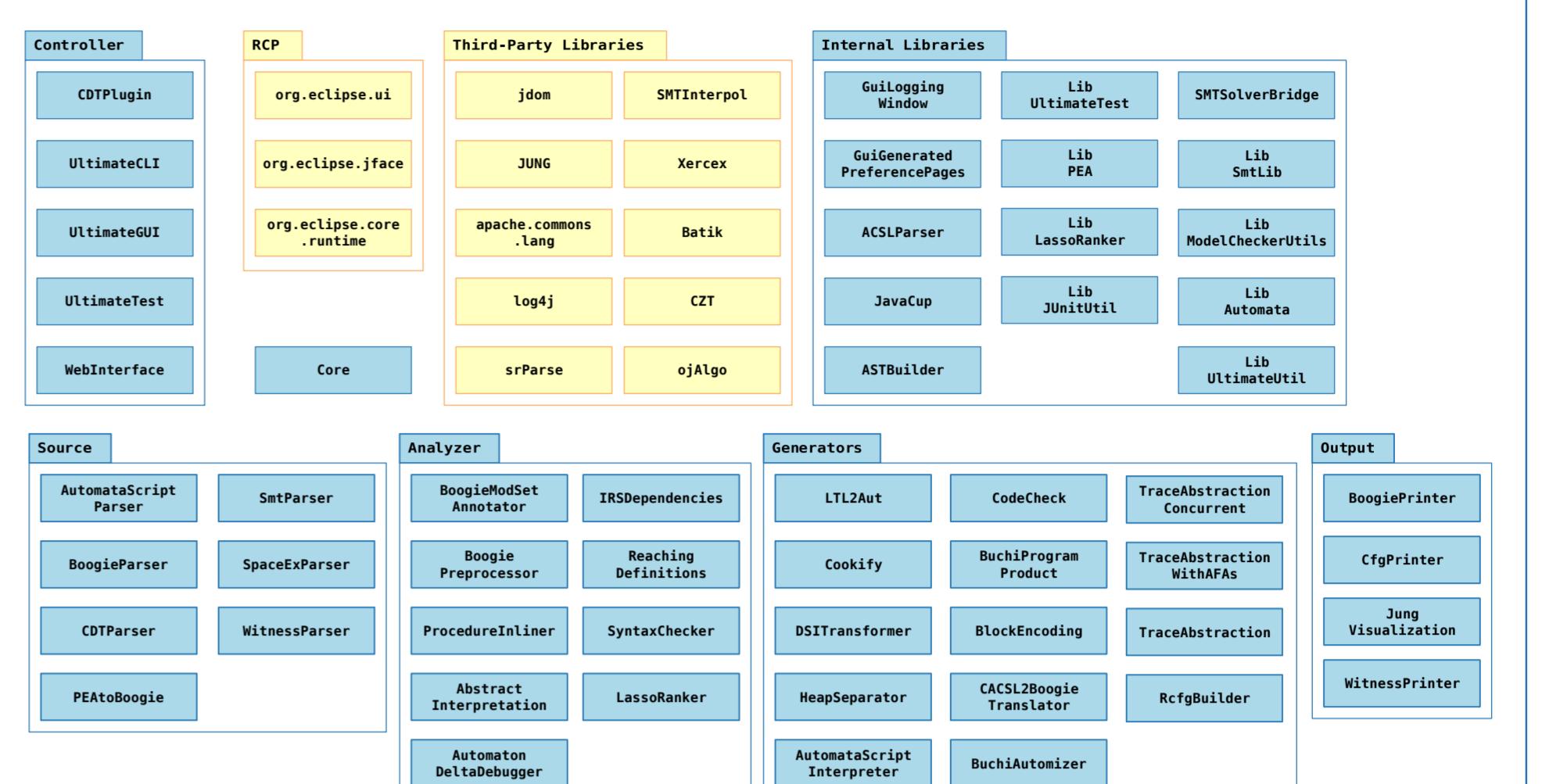
## Features

- Memory safety analysis
- Overflow detection
- Termination analysis using Büchi automata
- Nontermination analysis using geometric nontermination arguments
- LTL software model checking
- Bitprecise analysis
- IEEE 754 floating point analysis
- Error witnesses
- Correctness witnesses
- Error localization

## Techniques

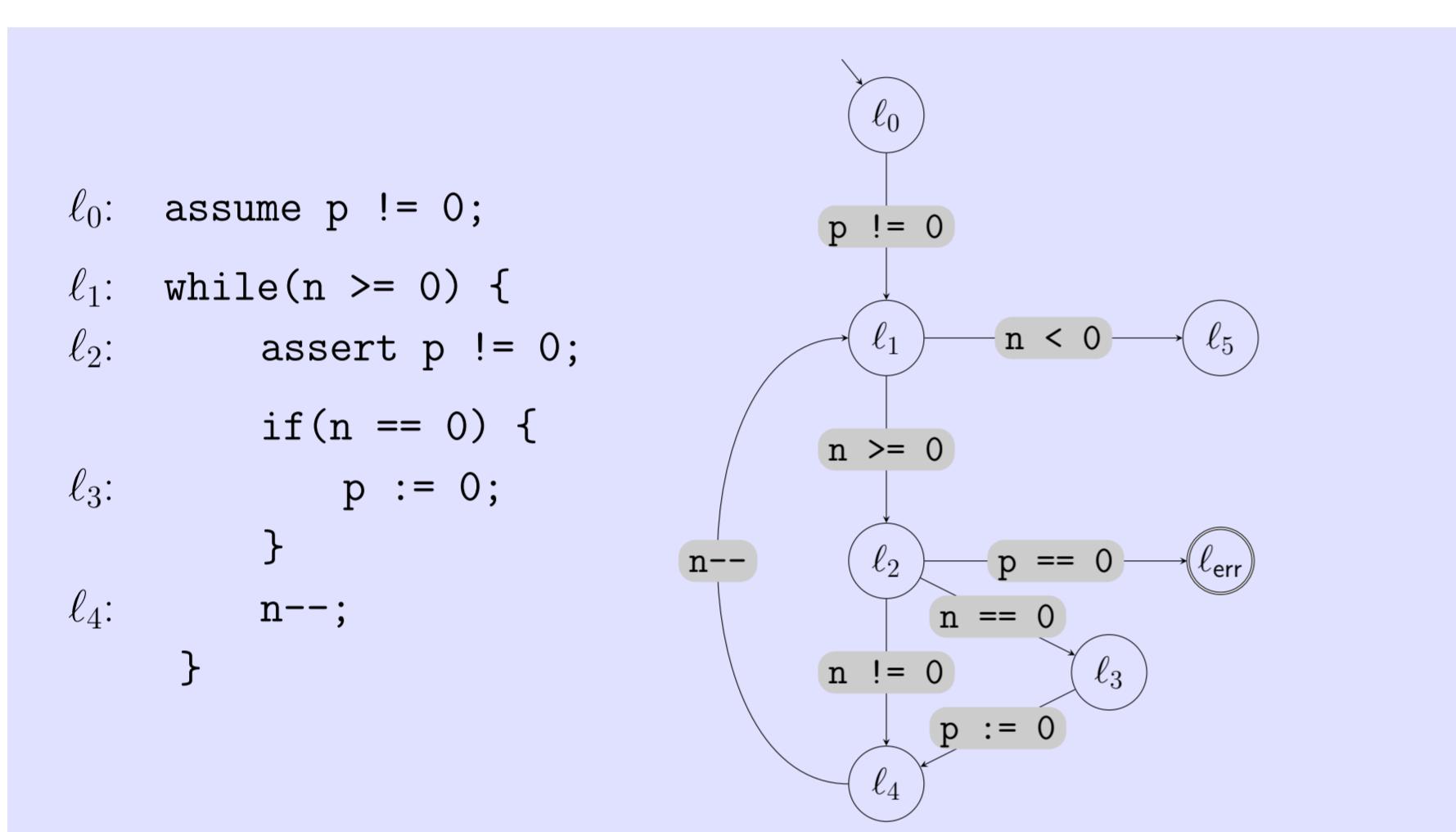
- On-demand trace-based decomposition
- Interprocedural analysis via nested word automata
- Theory-independent interpolation
- Refinement selection
- Configurable block encodings
- Multi SMT solver support
- Synthesis of ranking functions
- Efficient complementation of semi-deterministic Büchi automata
- (Nested word) automata minimization

## ULTIMATE program analysis framework



## Automata-theoretic proof of program correctness

Program  $\mathcal{P}$  is correct because each error trace is infeasible, i.e. the inclusion  $\mathcal{P} \subseteq \mathcal{A}_1 \cup \mathcal{A}_2$  holds.



- Alphabet: set of program statements  
 $\Sigma = \{ p \neq 0, n < 0, n \geq 0, p == 0, n == 0, n \neq 0, p := 0, n -- \}$

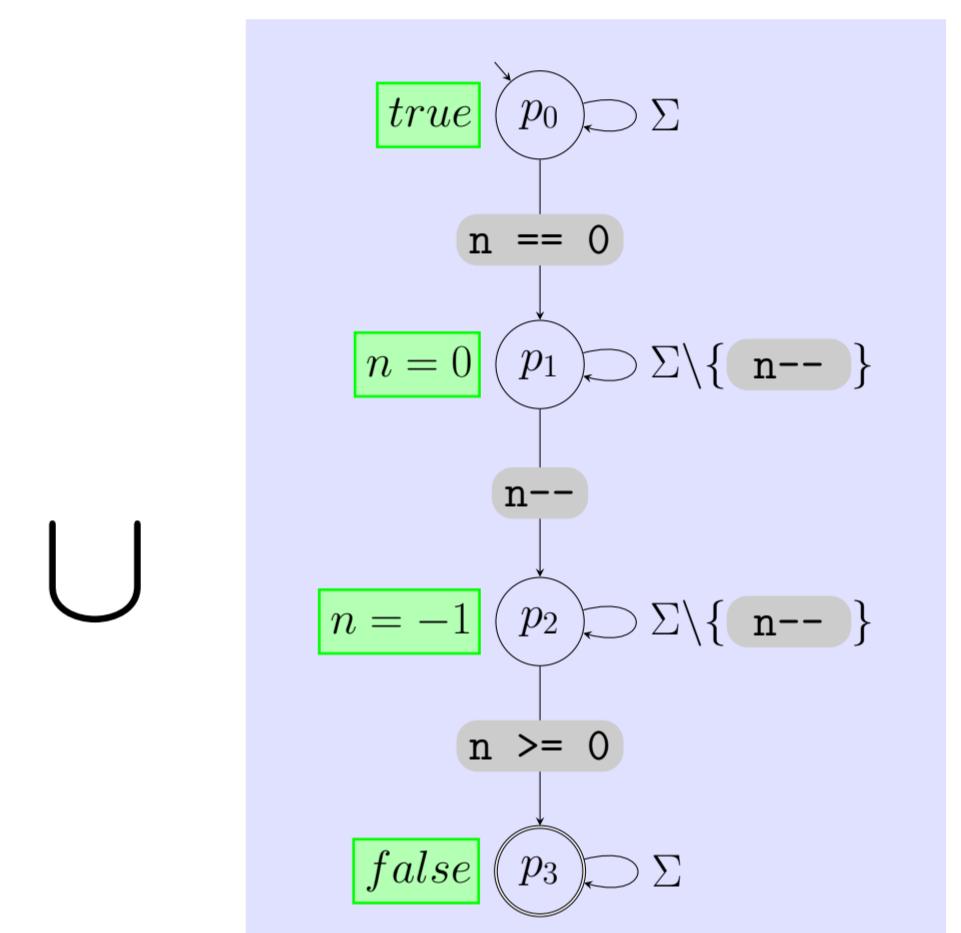
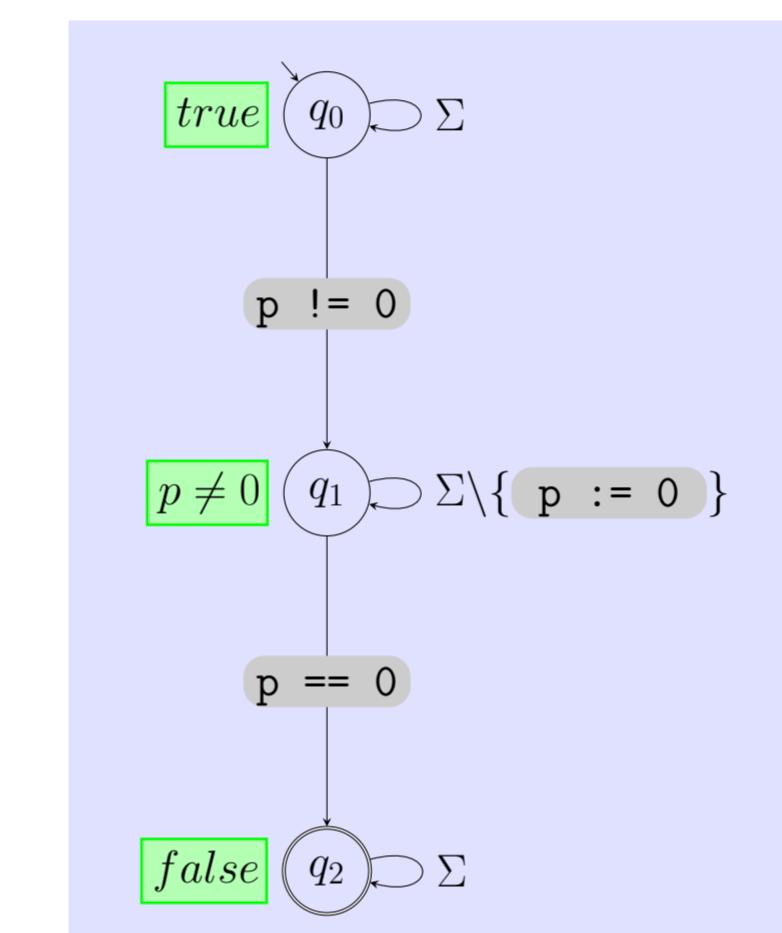
- The language of  $\mathcal{P}$  is the set of error traces.

- In the first iteration, we analyze feasibility of the error trace  $\pi_1 = p \neq 0 \ n \geq 0 \ p == 0$ .  $\pi_1$  is infeasible. Via interpolation, we obtain the following Hoare triples.

$$\begin{array}{lll} \{\text{true}\} & p \neq 0 & \{p \neq 0\} \\ \{p \neq 0\} & n \geq 0 & \{p \neq 0\} \\ \{p \neq 0\} & p == 0 & \{p \neq 0\} \end{array}$$

We construct the automaton  $\mathcal{A}_1$  such that its language is the set of all traces whose infeasibility can be shown using the predicates `true`, `p ≠ 0`, and `false`.

- Analogously, in the second iteration the automaton  $\mathcal{A}_2$  is constructed.
- We check the inclusion  $\mathcal{P} \subseteq \mathcal{A}_1 \cup \mathcal{A}_2$  and conclude that each error trace is infeasible and hence  $\mathcal{P}$  is correct.



**Definition** Given an automaton  $\mathcal{A} = (Q, \delta, q_{\text{init}}, Q_{\text{final}})$  over the alphabet of program statements, we call a mapping that assigns to each state  $q \in Q$  a predicate  $\varphi_q$  a *Floyd-Hoare annotation for automaton  $\mathcal{A}$*  if the following implications hold.

$$\begin{aligned} (q, s, q') \in \delta &\implies \{\varphi_q\} s \{ \varphi_{q'} \} \text{ is a valid Hoare triple} \\ q = q_{\text{init}} &\implies \varphi_q = \text{true} \\ q \in Q_{\text{final}} &\implies \varphi_q = \text{false} \end{aligned}$$

**Theorem** If an automaton  $\mathcal{A}$  has a Floyd-Hoare annotation, then  $\mathcal{A}$  recognizes a set of infeasible traces.

## Interpolation with unsatisfiable cores

Level 1: “interpolation” via

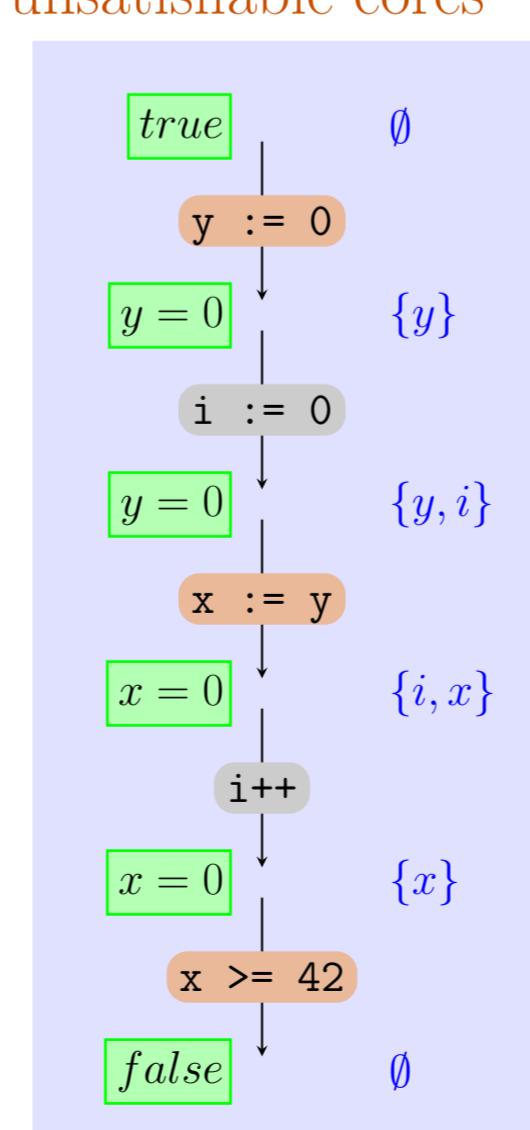
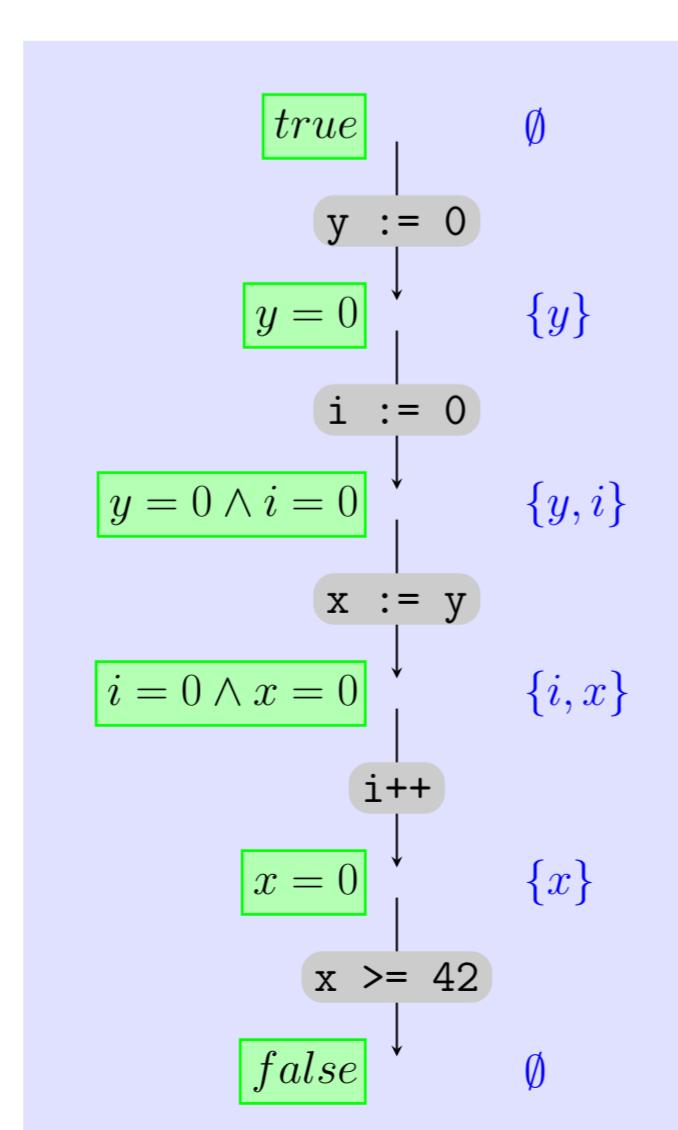
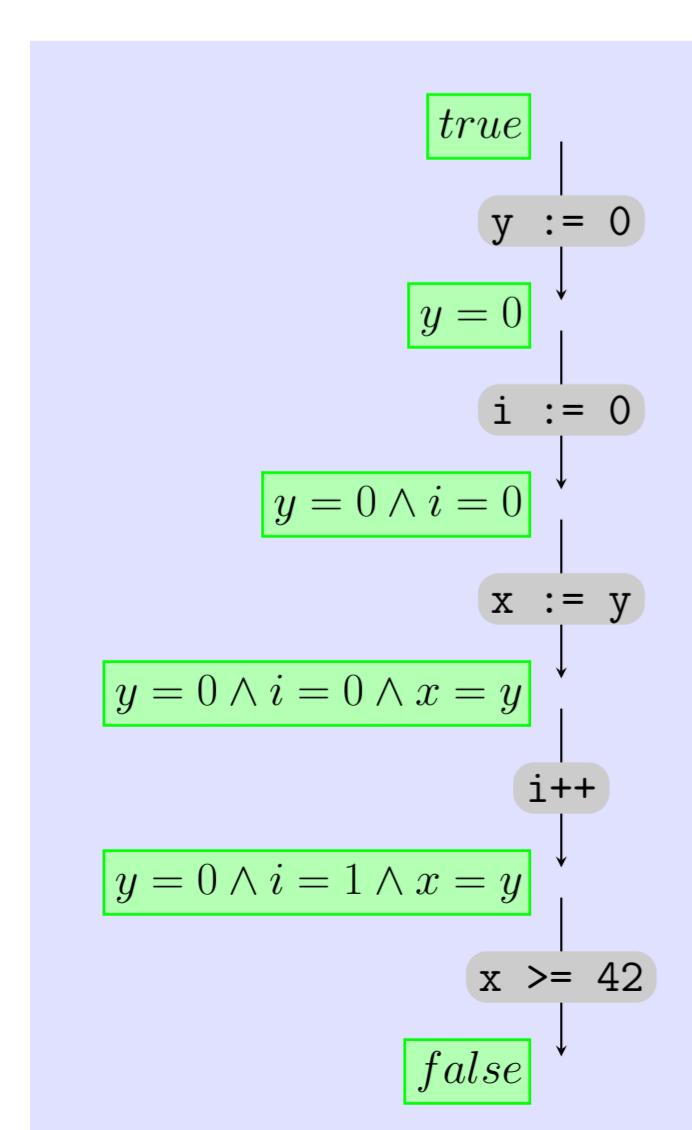
- strongest post

Level 2: interpolation via

- strongest post
- live variable analysis

Level 3: interpolation via

- strongest post
- live variable analysis
- unsatisfiable cores



Algorithm (for level 3)

- Input: infeasible trace  $s_1, \dots, s_n$  and unsatisfiable core  $UC \subseteq \{s_1, \dots, s_n\}$
- Replace each statement that does not occur in  $UC$  by a skip statement or a havoc statement.

assume statement  $\psi \rightsquigarrow \text{skip}$   
assignment statement  $x := t \rightsquigarrow \text{havoc } x$

- Compute sequence of predicates  $\varphi_0, \dots, \varphi_n$  iteratively using the strongest post predicate transformer.  $sp$

$$\begin{aligned} \varphi_0 &:= \text{true} \\ \varphi_{i+1} &:= sp(\varphi_i, s_{i+1}) \end{aligned}$$

- Eliminate each variable from predicate  $\varphi_i$  that is not live at position  $i$  of the trace.
- Output: sequence of predicates  $\varphi_0, \dots, \varphi_n$  which is a sequence of interpolants for the infeasible trace  $s_1, \dots, s_n$